## Coulomb Excitation of Light Mercury Isotopes

The study of shape-coexistence near the $Z=82$ shell closure

## Liam Gaffney



## Introduction

* Shape coexistence discovered over 30 years ago
* 0+ states: heads of differently shaped intrinsic structures
* 186 Pb : triplet of $0+$ states
* Particle hole configurations

Spherical Prolate Oblate
Op-0h $\quad 2 p-2 h \quad 4 p-4 h$

A. N. Andreyev, Nature 405 (2000) Pg 430-433

## Introduction • Mercury

* Protons excited across $Z=82$ shell gap driving deformation
* Ground state predicted slightly oblate, excited band prolate
* Model-independent determination of quadrupole moment, $Q_{0}$, required
* Sign of diagonal matrix-elements obtained from Coulomb Excitation

S. Fravendorf and V.V. Pashkevich Phys. Lett. 5534 (1974)


## Introduction • Mercury

* Protons excited across $Z=82$ shell gap driving deformation
* Ground state predicted slightly oblate, excited band prolate
* Model-independent determination of quadrupole moment, $Q_{0}$, required
* Sign of diagonal matrix-elements obtained from Coulomb Excitation

${ }^{184} \mathbf{H g}$
$29_{9 / 2}$
$N=126$
$3 p_{1 / 2}$
$2 f_{5 / 2}$
$3 p_{32}$

$v=104$
S. Fravendorf and V.V. Pashkevich Phys. Lett. 5584 (1974)


## Introduction • Mercury

* Protons excited across $Z=82$ shell gap driving deformation
* Ground state predicted slightly oblate, excited band prolate
* Model-independent determination of quadrupole moment, $Q_{0}$, required
* Sign of diagonal matrix-elements obtained from Coulomb Excitation

S. Fravendorf and V.V. Pashkevich Phys. Lett. 5584 (1974)


## Introduction • Coulex

${ }^{112} \mathrm{Cd}\left({ }^{184} \mathrm{Hg},{ }^{184} \mathrm{Hg}^{*}\right){ }^{112} \mathrm{Cd}^{*}$

* Inelastic scattering involving EM force
* Cross-section sensitive to quadrupole moment
* Different angular ranges exploits dependence
* Vary matrix elements to reproduce $\gamma$-ray yields



## Introduction • Coulex

${ }^{112} \mathrm{Cd}\left({ }^{184} \mathrm{Hg},{ }^{184} \mathrm{Hg}^{*}\right){ }^{112} \mathrm{Cd}^{*}$

* Inelastic scattering involving EM force
* Cross-section sensitive to quadrupole moment
* Different angular ranges exploits dependence
* Vary matrix elements to reproduce $\gamma$-ray yields



## Experimental Set-up

* REX-ISOLDE delivers > 600 isotopes post-accelerated up to 3.2 A.MeV to MINIBALL
* PS Booster: 1 or 1.4 GeV protons on molten Pb primary target
* REXTRAP/EBIS: trap, bunch and charge breed ions to $4 \leq A / q \leq 5$
* REX-Linac: Mass separator RFQ, IHS, 7-gap and 9-gap



## Experimental Set-up

* MINIBALL - 8 triple cluster Ge detectors, 6-fold segmentation
* $\varepsilon>7 \%$ at 1.3 MeV FWHM $=7 \mathrm{keV}$


Projectile - Hg

* DSSSD gives $\theta, \varphi$
and energy loss information



## Analysis • Kinematics

* Inverse kinematics reaction

* Identify products in Energy vs. Angle plot
* Gates on projectile define coincident $\gamma$-rays
* Coincident target particle kinematically reconstructed for Doppler correction



## Analysis • Kinematics

* Inverse kinematics reaction

* Identify products in Energy vs. Angle plot
* Gates on projectile define coincident $\gamma$-rays
* Coincident target particle kinematically reconstructed for Doppler correction



## Analysis ' Spectra






## Analysis • 2 Particle

* 2 particles required in opposite quadrants
* Energy gate on target $\rightarrow$ beam
* 3 distinct angular ranges
* Better Doppler correction



## Analysis • 2 Particle

* 2 particles required in opposite quadrants
* Energy gate on target $->$ beam
* 3 distinct angular ranges
* Better Doppler correction



## Analysis • 2 Particle

* 2 particles required in opposite quadrants
* Energy gate on target $\rightarrow$ beam
* 3 distinct angular ranges
* Better Doppler correction



## Analysis - 2 Particle

* 2 particles required in opposite quadrants
* Energy gate on target $\rightarrow$ beam
* 3 distinct angular ranges
* Better Doppler correction



## Analysis • 2 Particle

* 2 particles required in opposite quadrants
* Energy gate on target $\rightarrow$ beam
* 3 distinct angular ranges
* Better Doppler correction



## Analysis • 2 Particle

* 2 particles required in opposite quadrants
* Energy gate on target $\rightarrow$ beam
* 3 distinct angular ranges
* Better Doppler correction

Gate on target in low centre of mass angular range


## Analysis • p-p- $\gamma$



## Analysis ' Spectra



## Analysis • Minimisation

CALCULATED LIFETIMES

* GOSIA least squares fit Fortran code
* Error analysis yet to be performed
* Preliminary ${ }^{184} \mathrm{Hg}$ matrix elements:
$\left\langle 2^{+}\right|\left|E(2) \| 0^{+}{ }_{g . s}\right\rangle=1.57 \mathrm{eb}$
$\tau=23.6 \mathrm{ps} \Rightarrow 30(7)$ ps Rudd et. al.
* EO(2+ $\left.2 \rightarrow 2^{+}+1\right)$ transition to be understood
* EO(O ${ }^{+} 2 \rightarrow \mathrm{O}^{+}{ }_{\mathrm{g} . \mathrm{s}}$ ) transition is negligible

| LEVEL | LIFETIME(PSEC) | EXP | ERROR |
| :---: | :---: | :---: | :--- |
|  |  |  |  |
| 2 | $-.1000 \mathrm{E}+01$ |  |  |
| 3 | $0.2355 \mathrm{E}+02$ | $0.3000 \mathrm{E}+02$ | $0.7000 \mathrm{E}+11$ |
| 4 | $0.1068 \mathrm{E}+04$ | $0.9000 \mathrm{E}+03$ | $0.3000 \mathrm{E}+13$ |
| 5 | $0.1248 \mathrm{E}+03$ |  |  |
| 6 | $0.2288 \mathrm{E}+02$ | $0.3280 \mathrm{E}+02$ | $0.3400 \mathrm{E}+11$ |
| 7 | $0.1018 \mathrm{E}+02$ | $0.8100 \mathrm{E}+01$ | $0.3100 \mathrm{E}+11$ |
| 8 | $0.7449 \mathrm{E}+00$ |  |  |
| 9 | $0.5479 \mathrm{E}-01$ |  |  |

MATRIX ELEMENTS

| MULTIPOLARITY=2 |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| INDEX | NF | NS | ME | RED. TRANS |
| 1 | 1 | 3 | 1.57219 | 0.49436 |
| 2 | 1 | 5 | 0.19856 | 0.00789 |
| 3 | 3 | 3 | 0.51657 | ********* |
| 4 | 3 | 4 | 0.22870 | 0.05230 |
| 5 | 3 | 5 | 0.87943 | 0.15468 |
| 6 | 3 | 6 | -3.69149 | 1.51412 |
| 7 | 3 | 8 | 2.21473 | 0.54500 |
| 8 | 4 | 6 | -0.25174 | 0.06704 |
| 9 | 5 | 5 | -0.36546 | ********* |
| 10 | 5 | 6 | 5.12651 | 2.92012 |
| 11 | 5 | 8 | -0.35359 | 0.01389 |
| 12 | 6 | 6 | -1.80823 | ********* |
| 13 | 6 | 7 | 4.62143 | 1.64289 |
| 14 | 6 | 8 | 0.56963 | 0.03605 |
| 15 | 6 | 9 | 2.90912 | 0.65100 |
| 16 | 7 | 7 | -1.84570 | ********* |
| 17 | 7 | 8 | 0.37800 | 0.01588 |
| 18 | 7 | 9 | -0.16572 | 0.06211 |
| 19 | 8 | 8 | 1.61731 | ********* |
| 20 | 8 | 9 | -4.97438 | 1.90342 |
| 21 | 9 | 9 | 1.77290 | ********* |
| MULLT IPOLARITY $=7$ |  |  |  |  |
| INDEX | NF | NS | ME | RED. TRANS |
| 22 | 2 | 4 | 0.05877 | 0.00345 |
| 23 | 3 | 5 | 0.26490 | 0.01403 |
| ********* END OF EXECUTION |  |  |  | ********** |

# Summary and Future Work 

* Preliminary matrix elements shown $\left({ }^{184} \mathrm{Hg}\right)$

\author{

* Initial indication of oblate/prolate
}
* Investigate $22^{+}->21^{+}$ E0/M1/E2 effect
* Error bars expected to span 0 when calculated
* Lifetime measurements planned at Argonne
* EO SAGE proposal accepted at JYFL
* Branching ratios, lifetimes and $\delta$ values add data points to fit


# IS452 Collaborators Coulex of 182, 184, 186, 188 Hg 

A. Petts ${ }^{1}$, N. Bree ${ }^{2}$, P.A. Butler ${ }^{1}$, P. Van Duppen², A. Andreyev², B. Bastin², A. Blazhev³, B. Bruyneel ${ }^{3}$, M. Carpenter ${ }^{4}$, J. Cederkäll ${ }^{5}$, E. Clement ${ }^{6}$, T.E. Cocolios ${ }^{2}$, J. Dirkin ${ }^{2}$, J. Eberth ${ }^{3}$, L. Fraile ${ }^{5}$, C. Fransen ${ }^{3}$, L.P. Gaffney ${ }^{1}$, T. Grahn¹, M. Guttormsen ${ }^{7}$, K. Hadynska ${ }^{8}$, R.-D. Herzberg ${ }^{1}$, M. Huyse ${ }^{2}$, D.G. Jenkins ${ }^{9}$, R. Julin ${ }^{10}$, S. Knapen ${ }^{2}$, Th. Kröll ${ }^{11}$, R. Krücken ${ }^{11}$, A.C. Larsen ${ }^{7}$, P. Marley ${ }^{9}$, P.J. Napiorkowski${ }^{8}$, J. Pakarinen ${ }^{1}$, N. Patronis ${ }^{2}$, P.J. Peura ${ }^{10}$, E. Piselli6, P. Reiter ${ }^{3}$, M. Scheck ${ }^{1}$, S. Siem ${ }^{7}$, I. Stefanescu ${ }^{2}$, J. Van de Walle ${ }^{6}$, D. Voulot ${ }^{6}$, N. Warr ${ }^{3}$, D. Weissharr ${ }^{3}$, F. Wenanders ${ }^{6}$, M. Zielinska ${ }^{9}$

1 Oliver Lodge Laboratory, Department of Physics, University of Liverpool, Liverpool, UK, 2 Instituut voor Kern- en Stralingsfysika, Katholieke Universiteit Leuven, B-3000 Leuven, Belgium<br>3 Institut für Kernphysik, Universität zu Köln, Zülpicher Str. 77, 50937 Köln, Germany<br>4 Argonne National Laboratory, Chicago Illonois<br>5 Department of Physics, Royal Institute of Technology, Stockholm, Sweden<br>6 CERN, Genève, Switzerland<br>7 Department of Physics, University of Oslo, P.O.Box 1048, Blindern, N-0316 Oslo, Norway<br>8 Heavy Ion Laboratory, University of Warsaw, Pasteura 5A, 02-093 Warszawa, Poland<br>9 Department of Physics, University of York, UK<br>10 Department of Physics, University of Jyväskylä, P.O.Box 35, 40014 Jyväskylä, Finland<br>11 Physik-Department E12, TU München, 85748 Garching, Germany

## Analysis - 2 Particle

Gate on target in low centre of mass angular range


## Analysis • 2 Particle



## Analysis - 2 Particle

Gate on target in low centre of mass angular range


## Analysis - 2 Particle

## Gate on target in mid centre of mass range



## Analysis - 2 Particle

## Gate on target in mid centre of mass range



## Analysis - 2 Particle

## Gate on target in mid centre of mass angular range



## Analysis - 2 Particle



## Analysis • 2 Particle



## Analysis - 2 Particle

Gate on target in high centre of mass angular range


