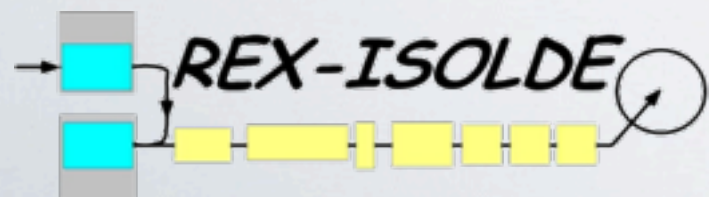


STUDY OF SHAPE COEXISTENCE IN NEUTRON DEFICIENT MERCURY ISOTOPES

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University of Liverpool



UNIVERSITY OF
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TALK OUTLINE

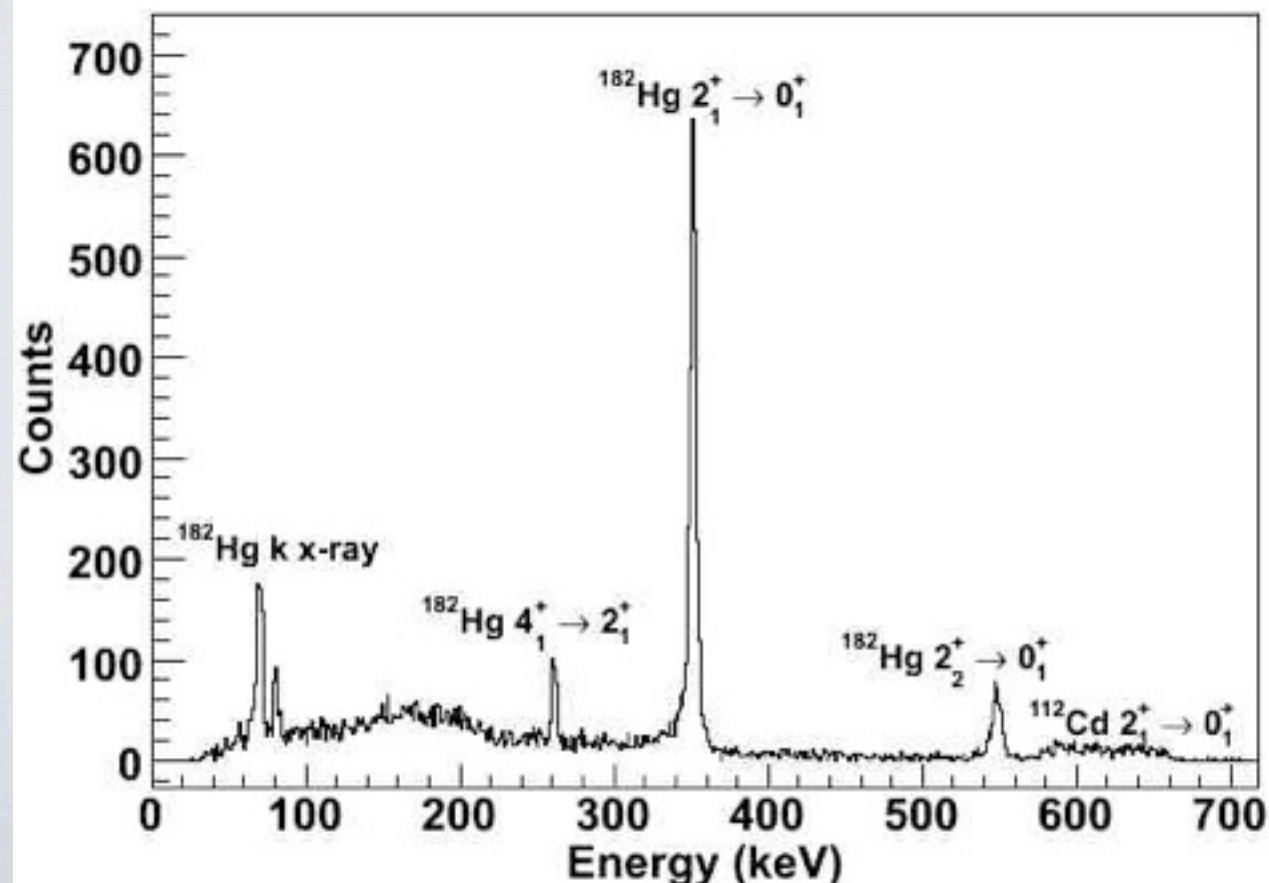
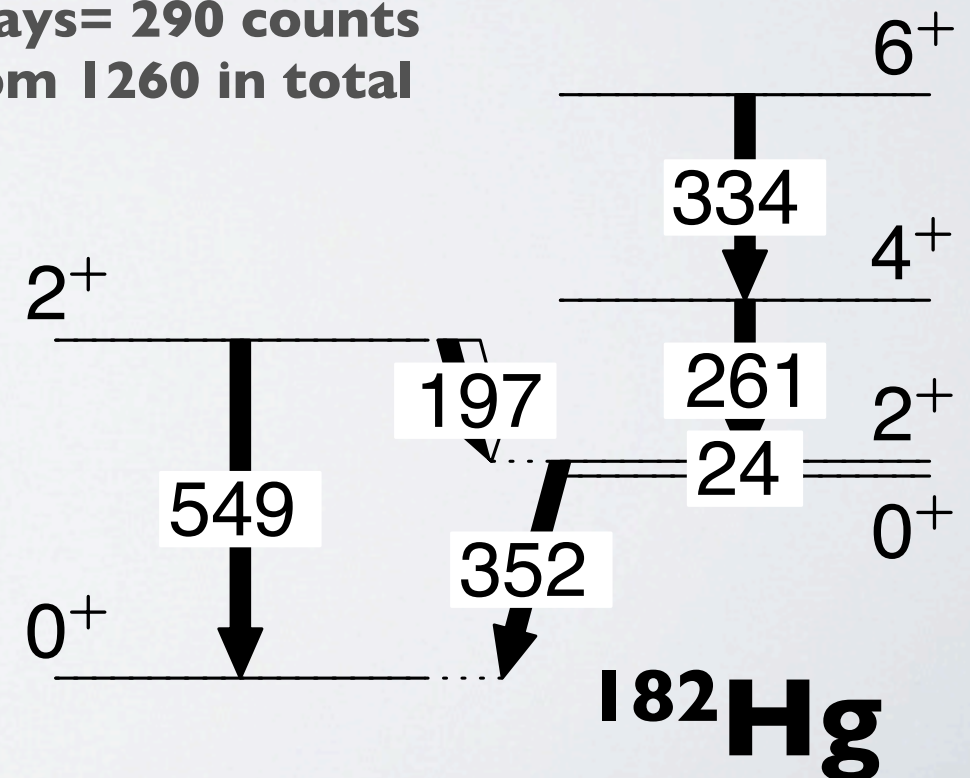
- X-ray analysis
- Effect of E0 component
- Lifetime measurements
- Matrix elements in $^{182,186}\text{Hg}$
- Future work and conclusions

X-RAY ANALYSIS

- Excess of x-rays are seen in $^{182,184}\text{Hg}$
- Source? - Attributed to E0 transitions
- $2_2^+ \rightarrow 2_1^+$ in coincidence with $2_1^+ \rightarrow 0_1^+$
- Xray = Internal Conversion + E0

Transition	Energy	Counts
Hg $2_1^+ \rightarrow 0_1^+$	351 keV	3591 ± 81
Hg $2_2^+ \rightarrow 0_1^+$	549 keV	510 ± 39
Hg $4_1^+ \rightarrow 2_1^+$	262 keV	321 ± 33
Hg $2_2^+ \rightarrow 2_1^+$	196 keV	101 ± 29
Hg k X-ray	68 keV	1260 ± 53
Cd $2_1^+ \rightarrow 0_1^+$	605 keV	768 ± 40

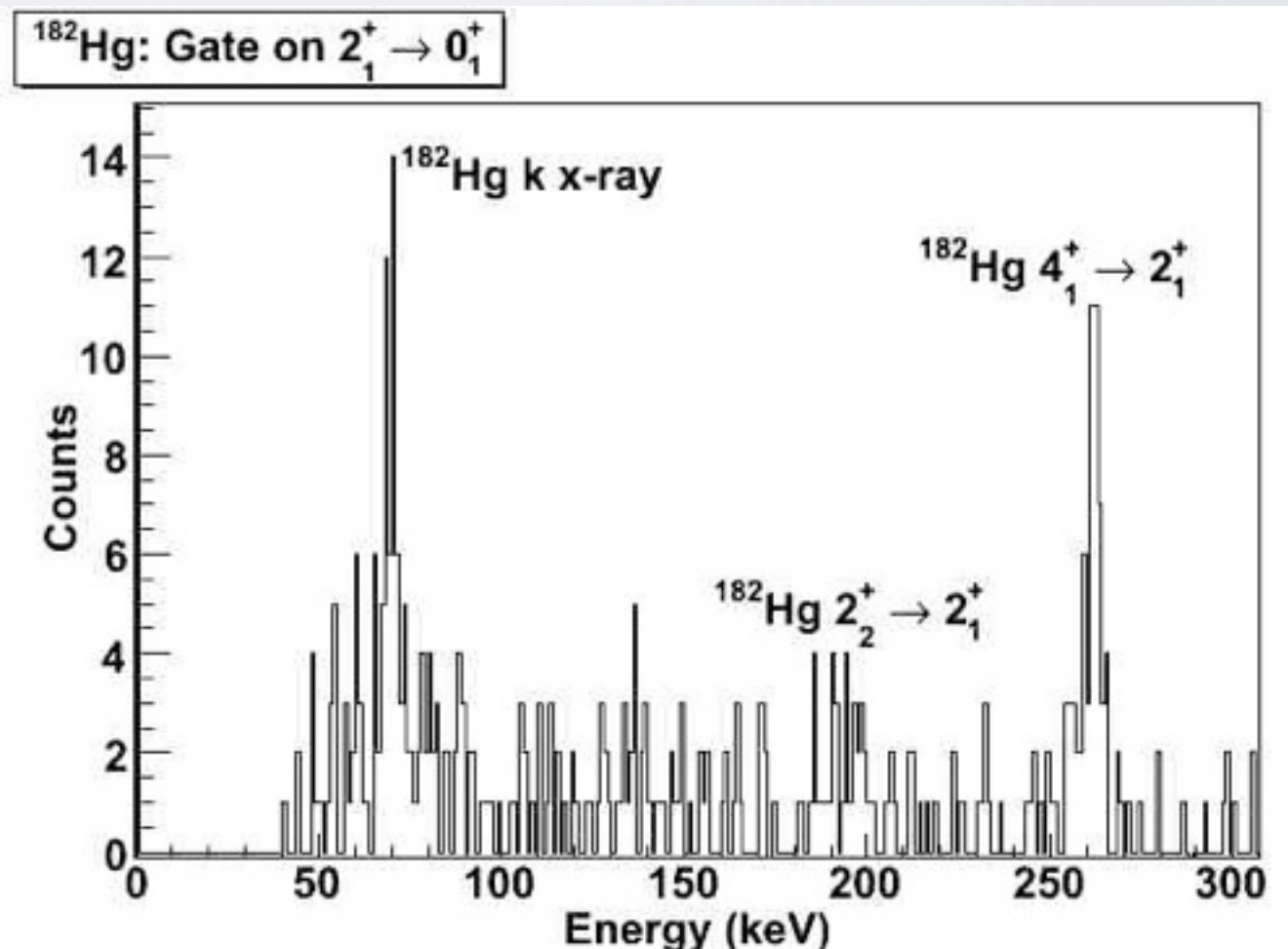
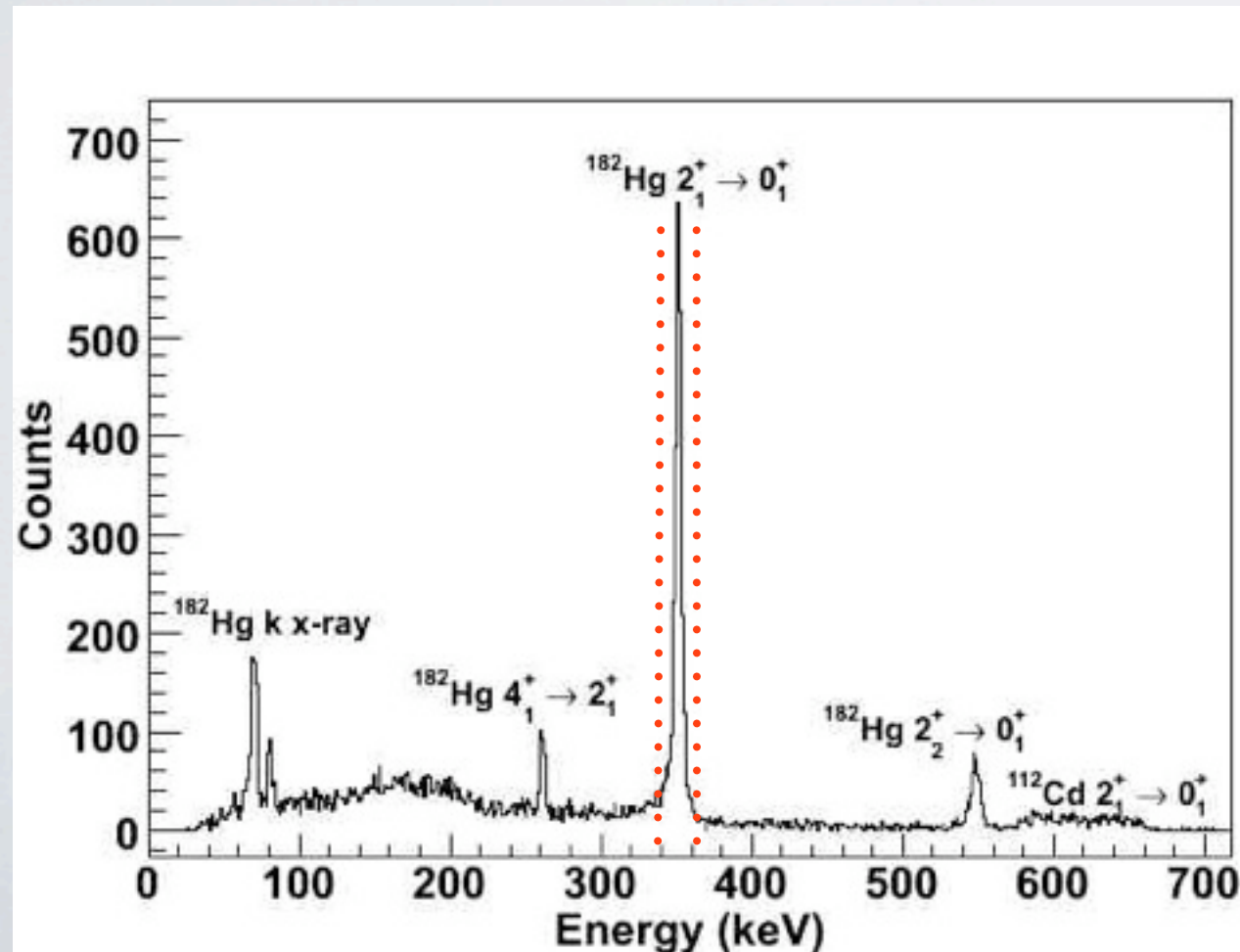
maximum internal conversion induced Xrays= 290 counts from 1260 in total



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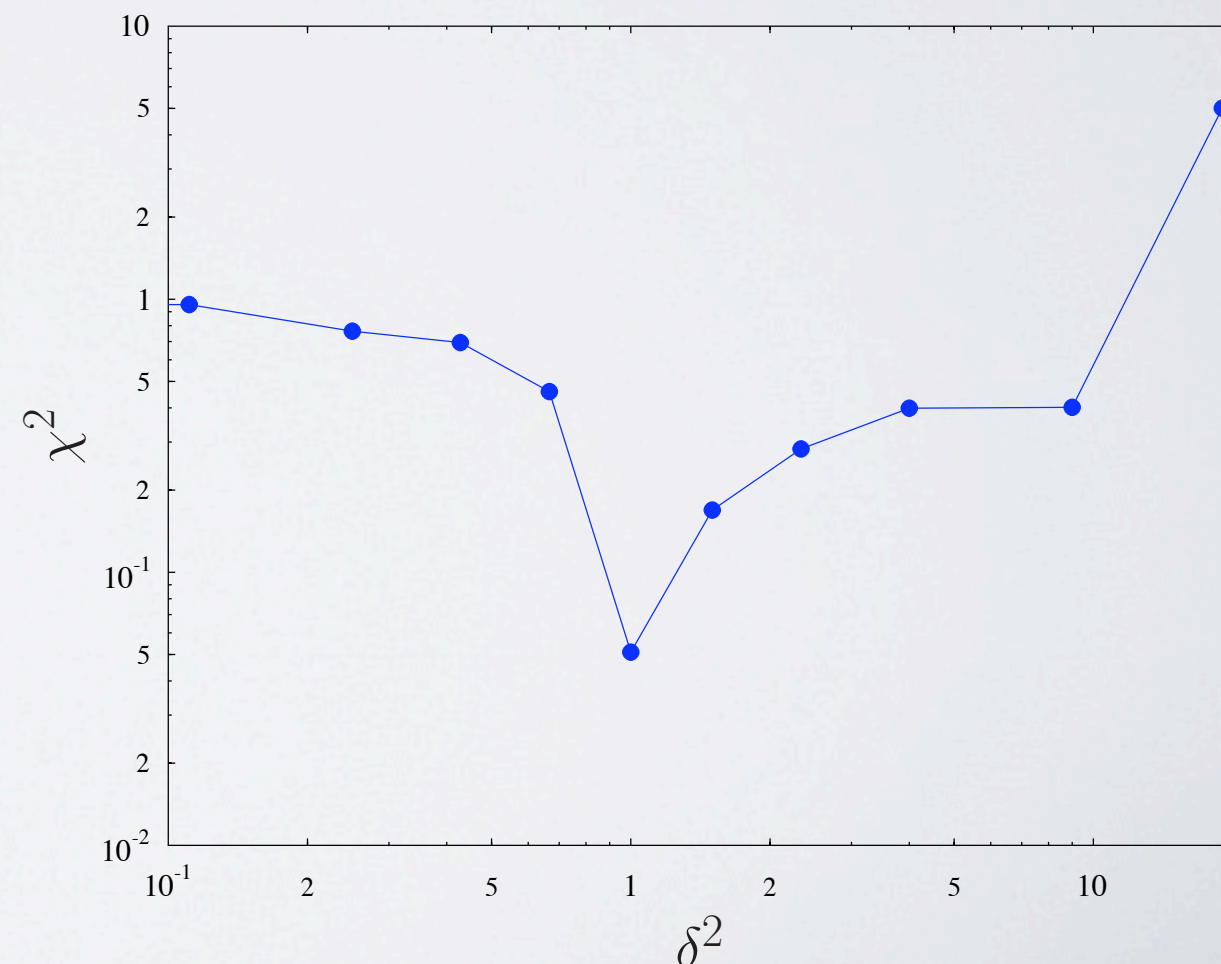
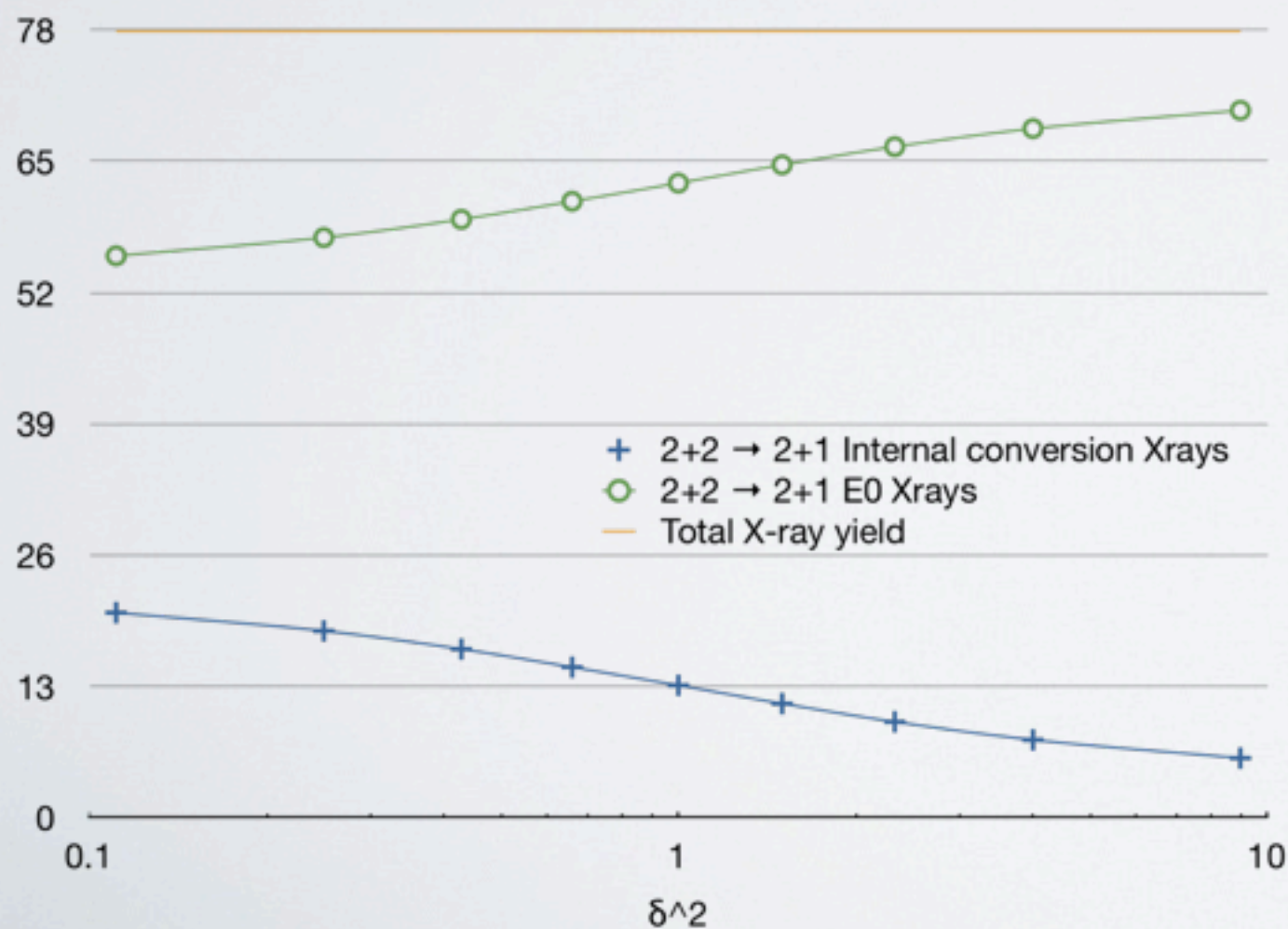
Transition	Energy	Counts
k x-ray	68 keV	78 ± 15
$2_2^+ \rightarrow 2_1^+$	196 keV	23.3 ± 5.2
$4_1^+ \rightarrow 2_1^+$	262 keV	62.9 ± 9.6



E0 ANALYSIS

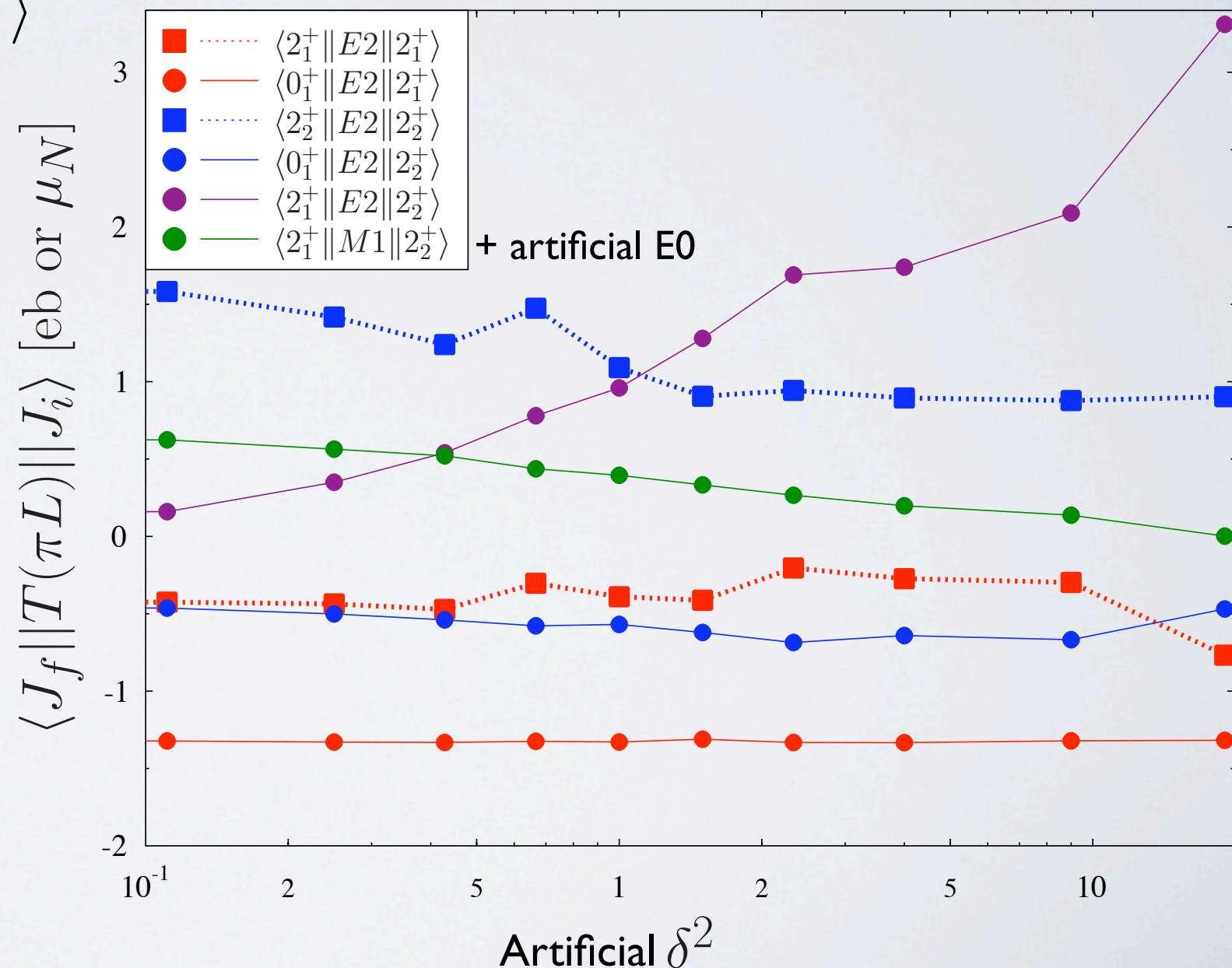
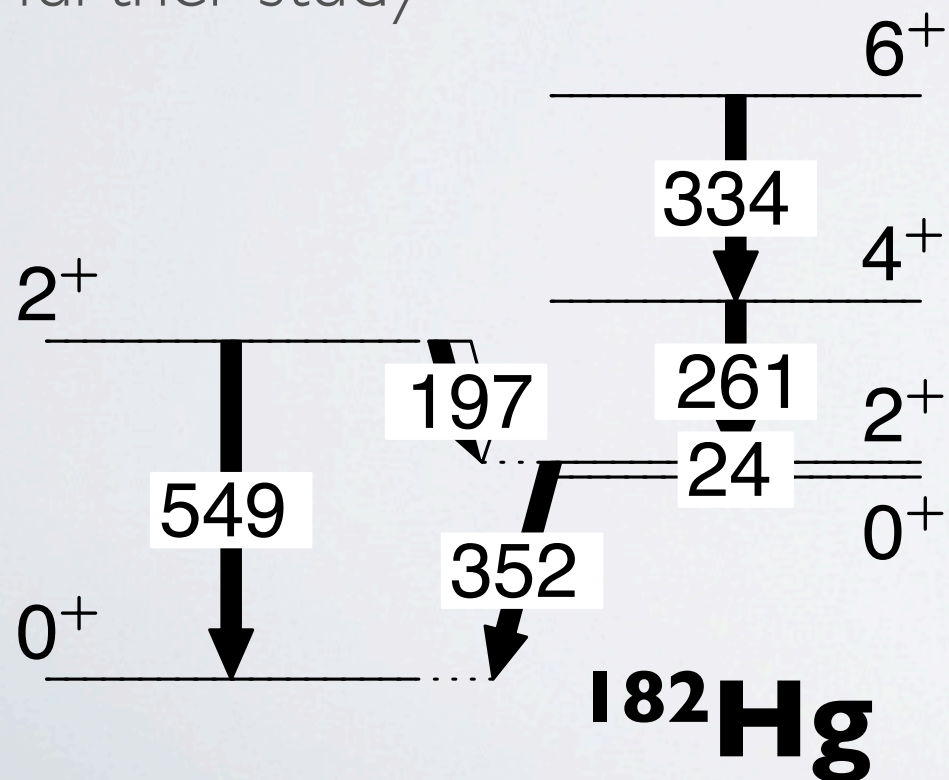
- Internal conversion of $2_2^+ \rightarrow 2_1^+$ depends on ratio of E2/M1, i.e. δ
- δ is unknown so how do we know the exact contribution?
- One needs to find solution which fits best in Gosia ... [Andrew Petts]

Assignment of Xrays in coincidence with $2+1 \rightarrow 0+1$



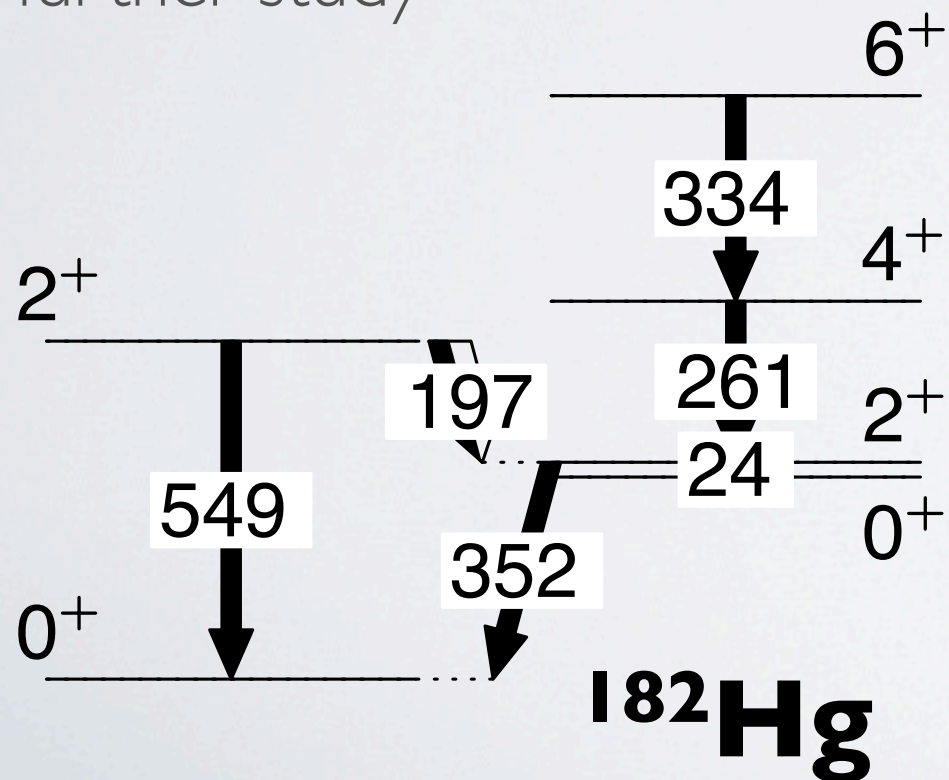
EFFECT OF E0 COMPONENT

- Additional E0 contribution mimicked by artificially increasing M1 component
- Variation of matrix elements not huge with variation of δ .
- Without E0 feeding $\langle 2_1^+ || E2 || 2_1^+ \rangle$ is shifted to small positive values
- Significant effect which needs further study

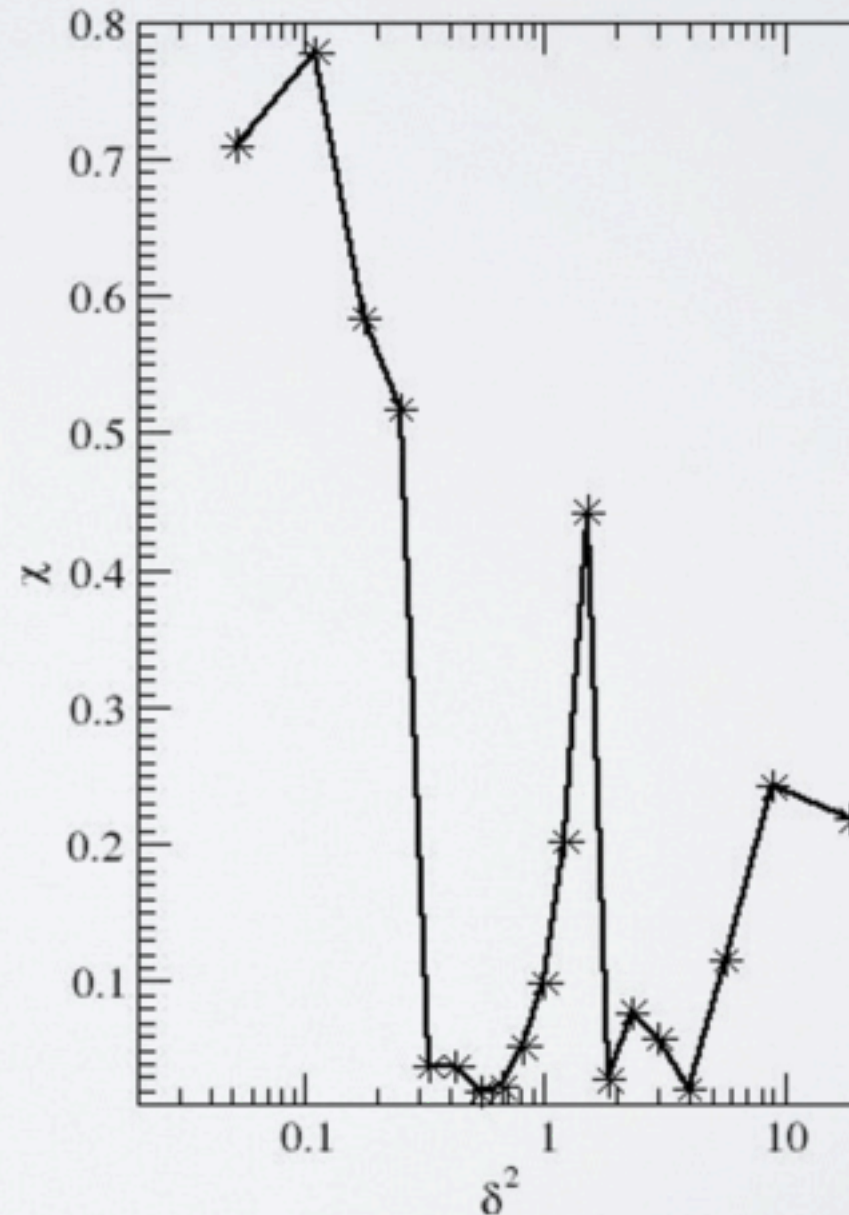


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Fixed δ^2 vs. Resulting χ^2



LIFETIME ANALYSIS

- Lifetimes of yrast states have been recently measured in $^{180,182}\text{Hg}$
- $^{184,186,188}\text{Hg}$ RDDS measurement took place recently at ANL using Gammasphere
- States $J^\pi \geq 2^+$ in $^{180,182}\text{Hg}$ have similarly structured wavefunctions
- Similar for $J^\pi \geq 4^+$ in $^{184,186}\text{Hg}$, indicating a difference between $J^\pi=2^+$ and $J^\pi=4^+$

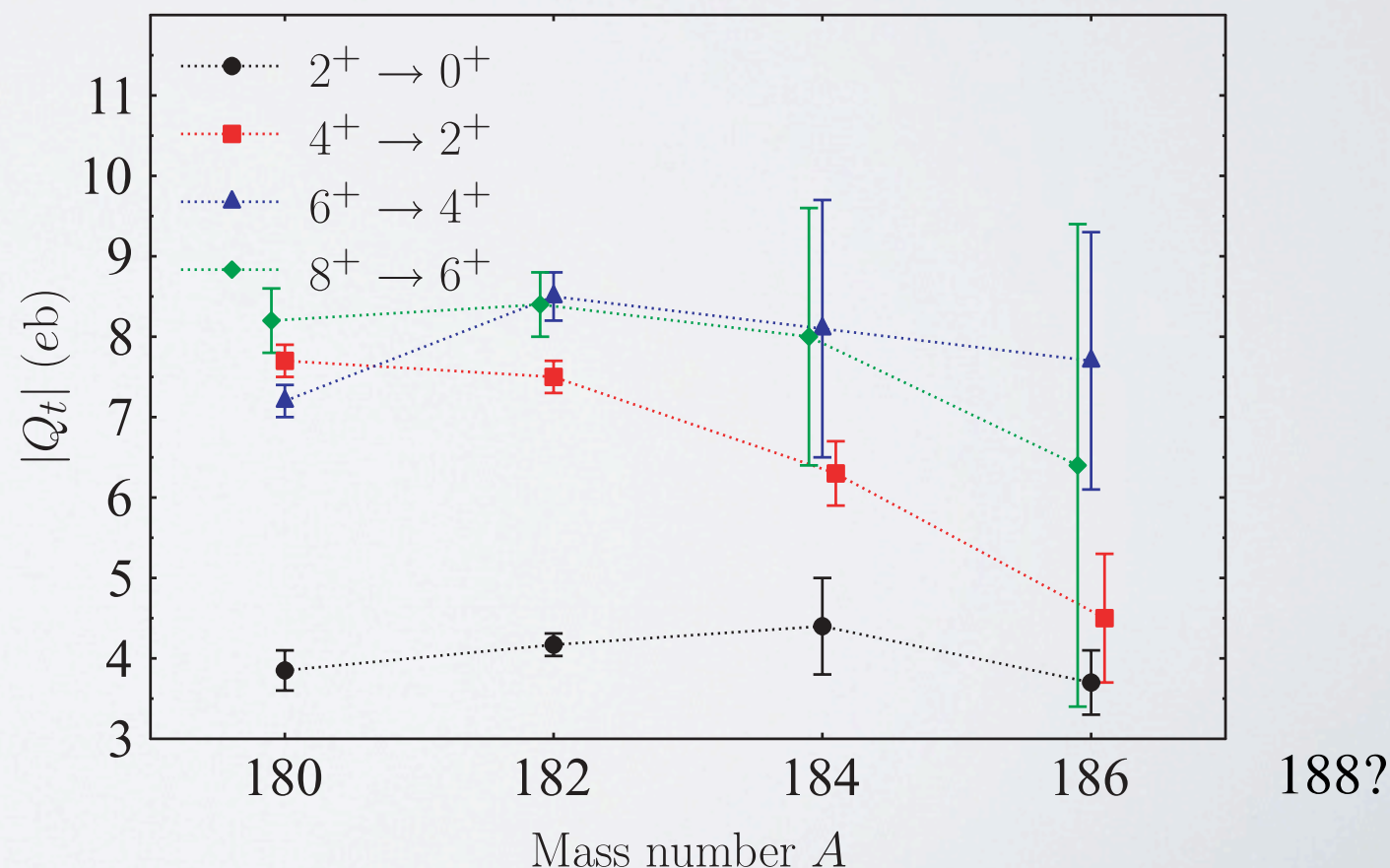
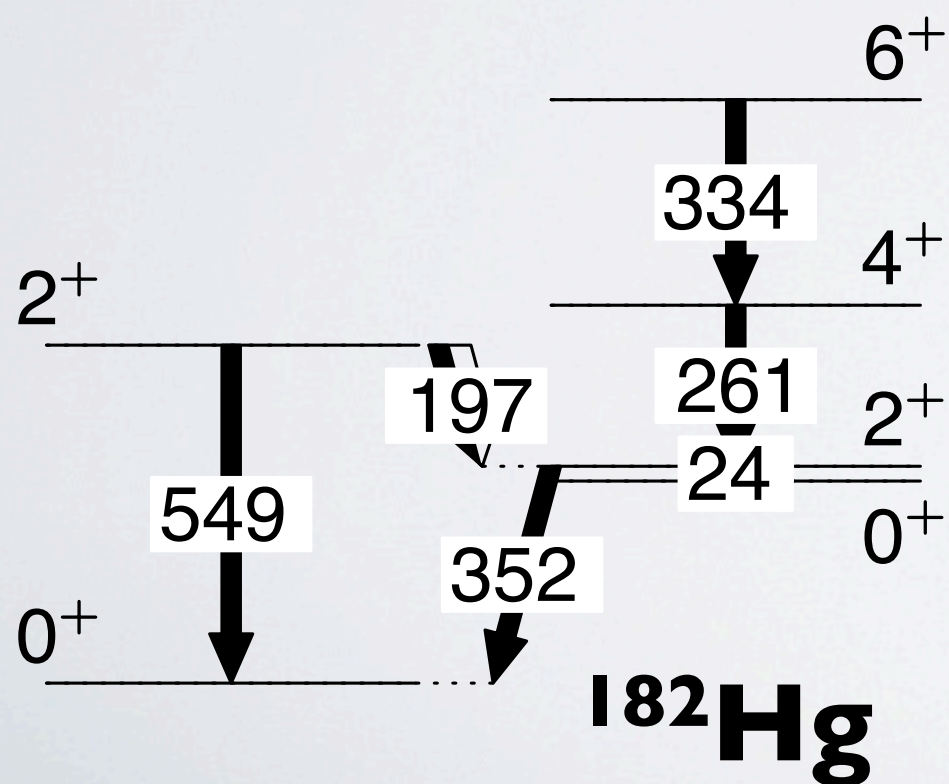


Figure: T. Grahn, A. Petts, M. Scheck et. al, Phys. Rev. C **80**, 014324 (2009)

^{182}Hg MATRIX ELEMENTS

- $\langle 2_1^+ \| E2 \| 2_1^+ \rangle$ varied and yield reproduced by matching $\langle 2_1^+ \| E2 \| 0_1^+ \rangle$
- Overlap region of 1 sigma suggests slightly -ive DME.

• GOSIA minimisation:

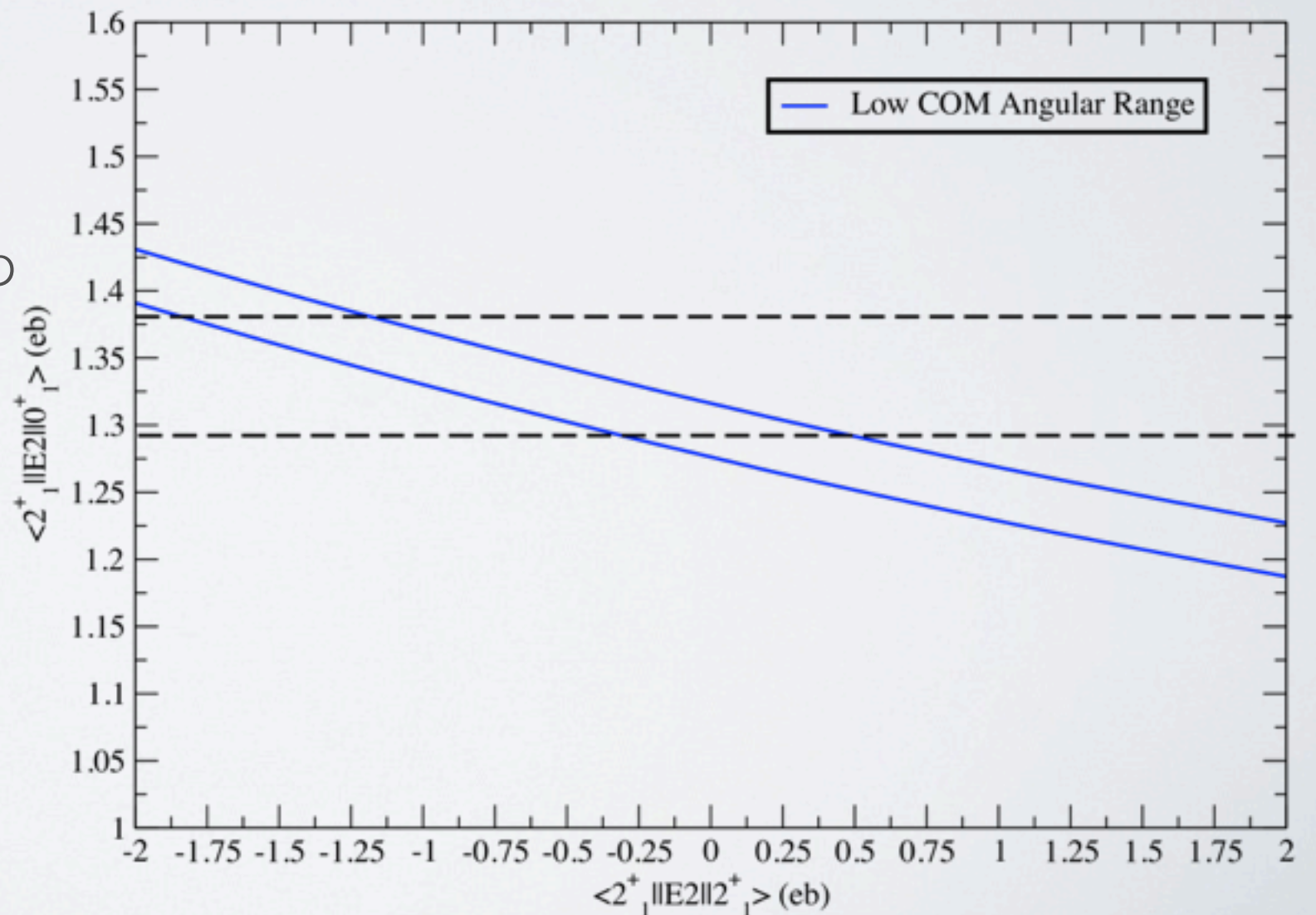
• $\langle 2_1^+ \| E2 \| 0_1^+ \rangle = (1.33 \pm 0.06) \text{ eb}$

• $\langle 2_1^+ \| E2 \| 2_1^+ \rangle = -(0.39 \pm 0.42) \text{ eb}$

• Suggestive of prolate

• Sensitivity restricts error bar

^{182}Hg 2_1^+ Hurst Plot



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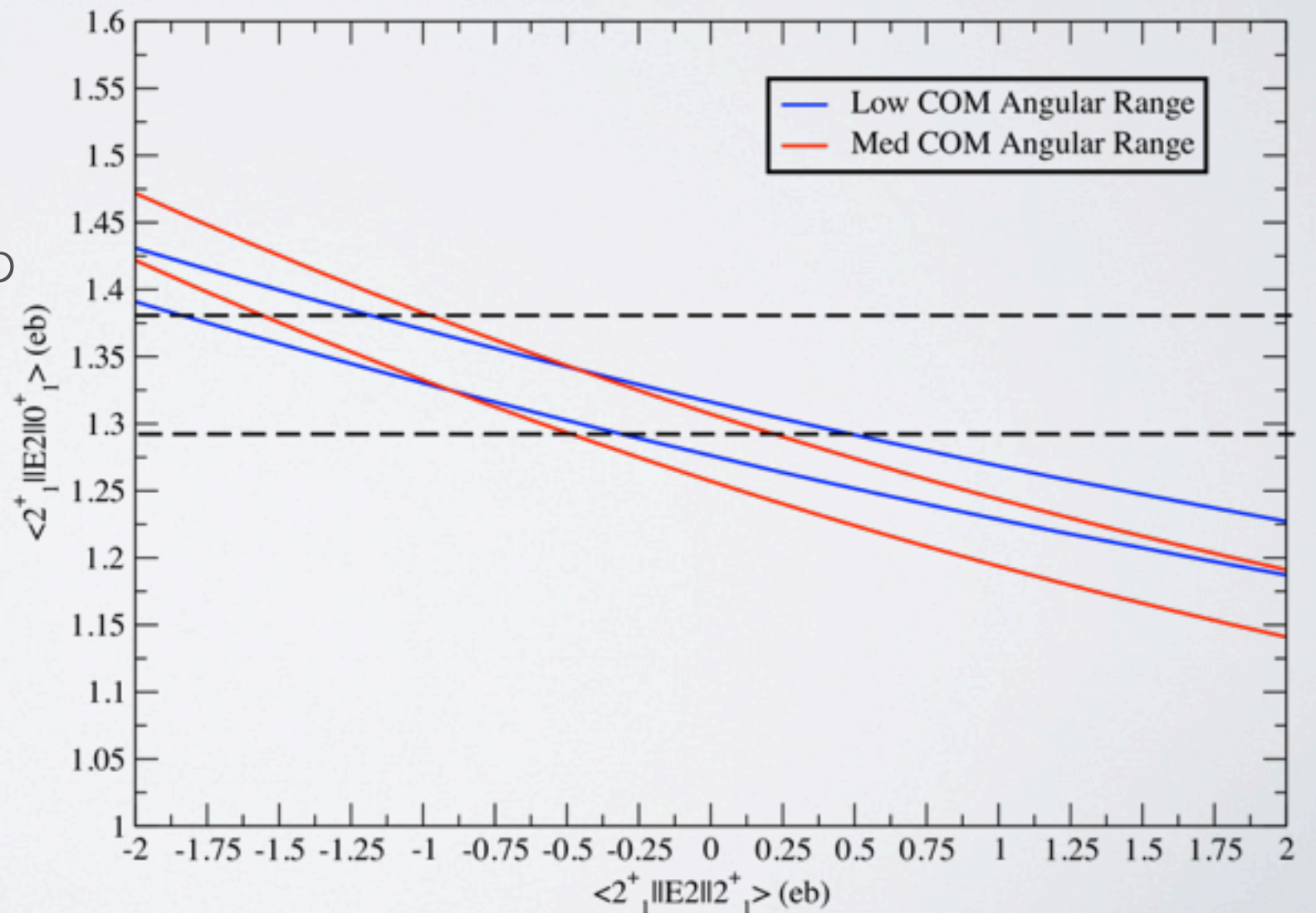
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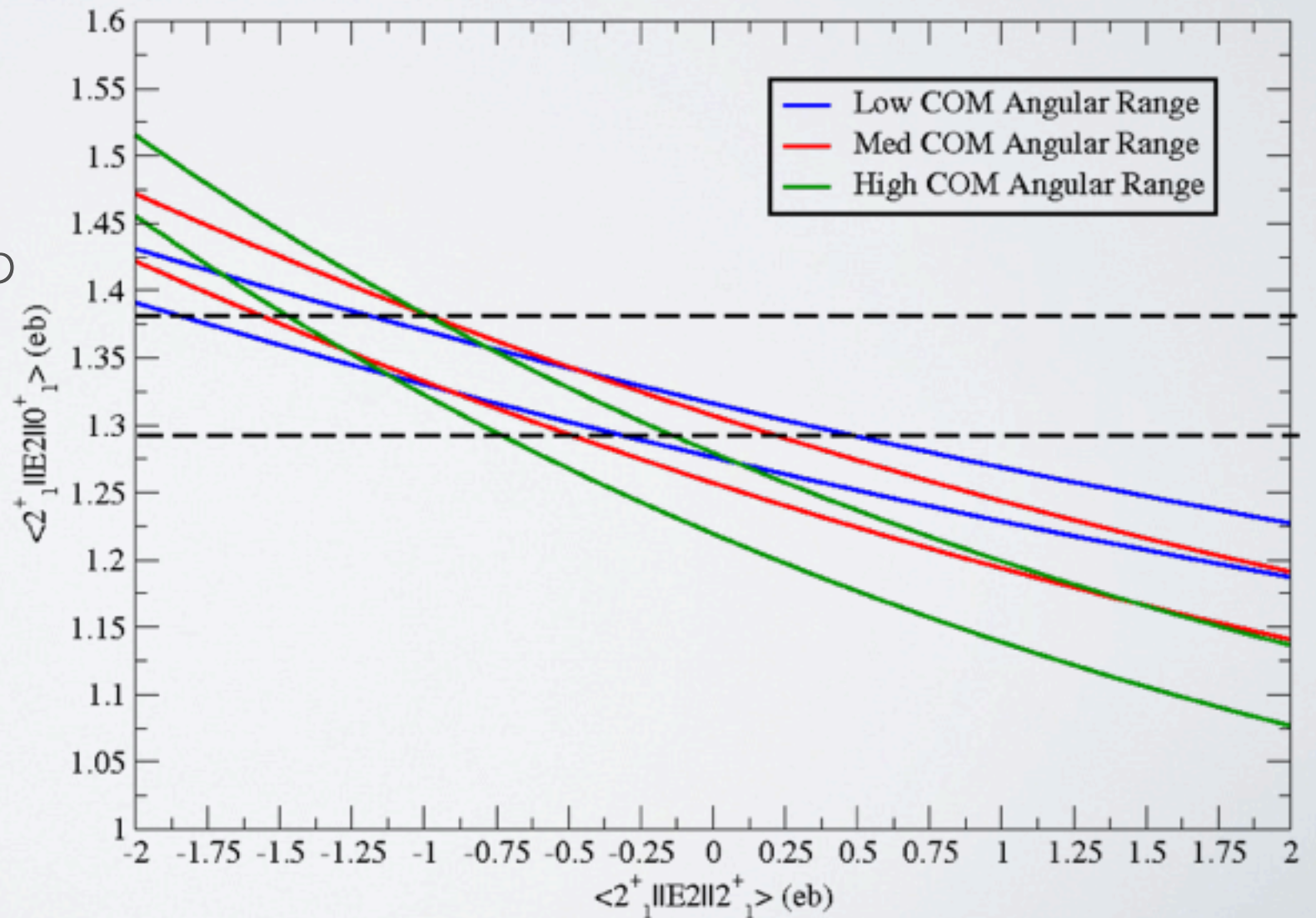
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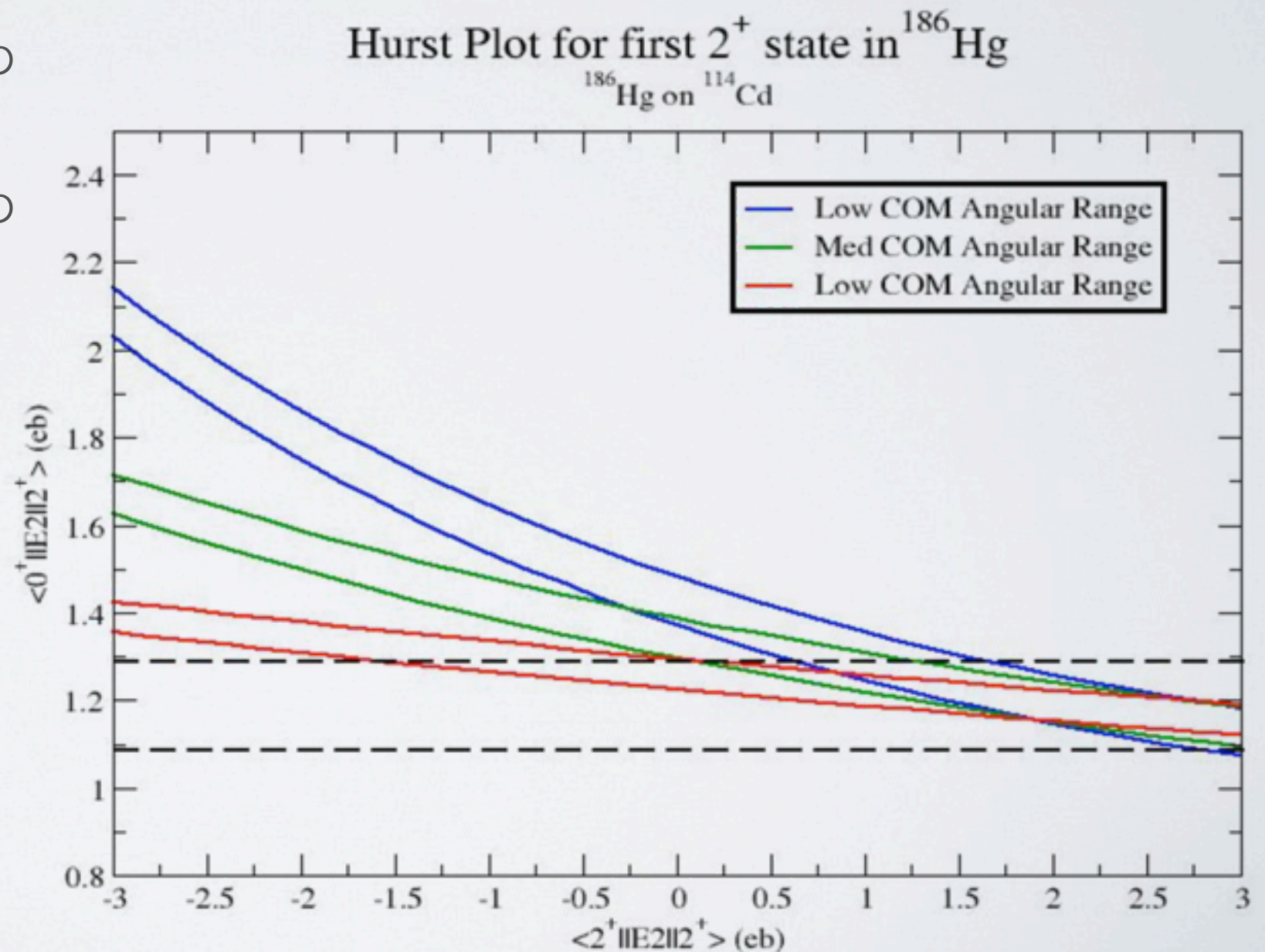
• Sensitivity restricts error bar

^{182}Hg 2_1^+ Hurst Plot



^{186}Hg MATRIX ELEMENTS

- More definitive positive DME suggested from simple view
- Gosia minimisation:
- $\langle 2_1^+ \| E2 \| 0_1^+ \rangle = (1.17 \pm 0.08) \text{ eb}$
- $\langle 2_1^+ \| E2 \| 2_1^+ \rangle = (1.89 \pm 0.64) \text{ eb}$
- Oblate deformation
- Supported by lifetime analysis



FUTURE WORK / CONCLUSIONS

- Diagonal and transitional matrix elements extracted in ^{182}Hg and ^{186}Hg by Andrew Petts from Coulex experiment with MINIBALL at REX-ISOLDE
- RDDS lifetime measurements in $^{184,186,188}\text{Hg}$ at Argonne just taken place using Köln plunger coupled with Gammasphere Ge array.
- E0 component to be studied using gamma-electron coincidences at Jyväskylä with the electron spectrometer, SAGE and the JUROGAM Ge array.
- Further analysis of Coulex data, reducing errors with new measurements.

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MIXING ANALYSIS

$$|u\rangle = \alpha|\text{oblate}\rangle + \beta|\text{prolate}\rangle$$

^{182}Hg		β (yrast)
0 ⁺ states:	α -hinderance	16%
	energy levels	7%
2 ⁺ states:	lifetimes	80%
	energy levels	70%
^{184}Hg		
0 ⁺ states:	α -hinderance	18%
	energy levels	5%
	E0 strength mixing	0.2%
2 ⁺ states:	energy levels	3%
^{186}Hg		
0 ⁺ states:	energy levels	3%
	E0 strength mixing	>4%
2 ⁺ states:	energy levels	8%
	E2 matrix elements	<10%

References:

Wauters et al. 1993, 1994
 Richards et al. 1997
 Grahn et al. 2009
 NNDC